



Insights from Macroscopic Models of Urban Transportation Systems

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References

1. Daganzo, C.F. (1996) "The nature of freeway gridlock and how to prevent it" in Transportation and Traffic Theory, Proc. 13th Int. Symp. Trans. Traffic Theory (J.B. Lesort, ed) pp. 629-646, Pergamon Elsevier, Tarrytown, N.Y.
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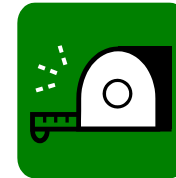
Approaches to City-Scale Modeling

- Disaggregate Model
 - Unavailable Inputs
 - Untestable Theories
- Aggregate Model
 - Observable Inputs
 - Testable Theories

Mountains of Data

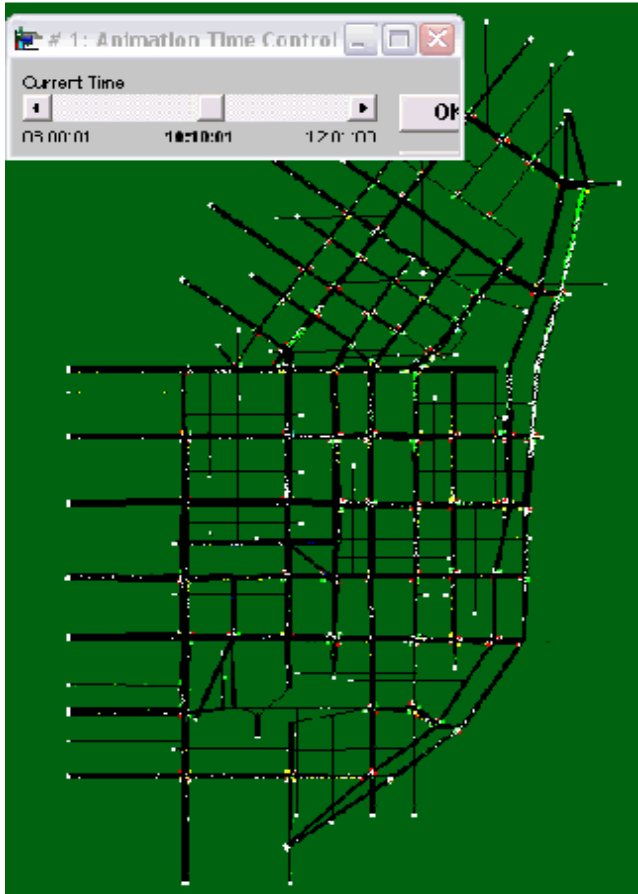


Measurable Data

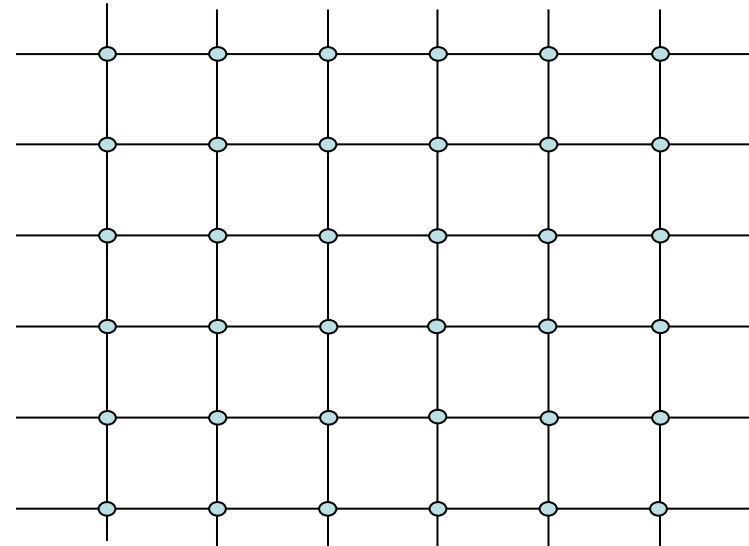


At the aggregate level,
we can find testable laws of behavior.

Aggregate Models of Traffic & Transit



Traffic Network



Transit Network

URBAN TRAFFIC: Two Conjectures

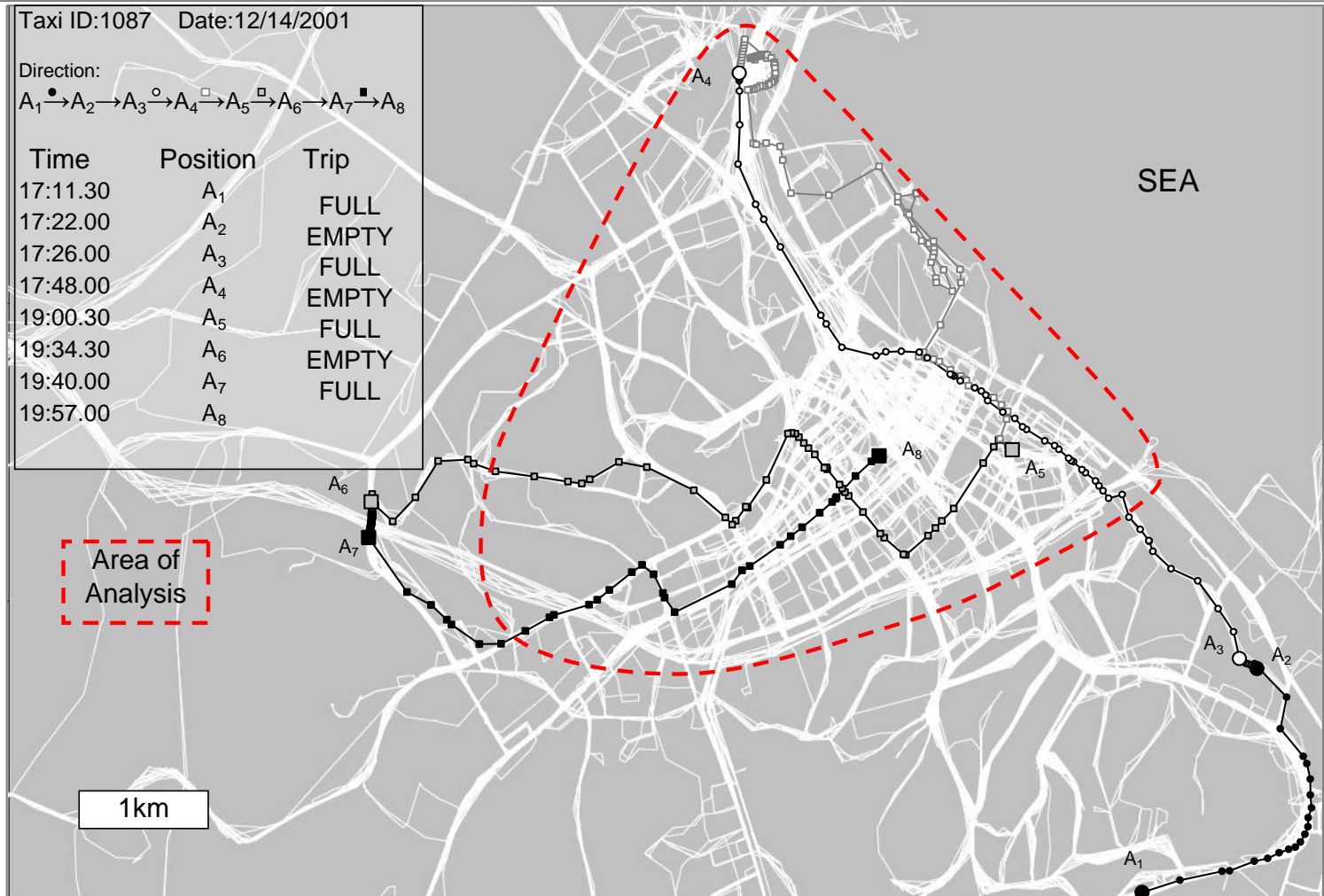
Hypothesis

If vehicles (i.e., congestion) are uniformly distributed in space

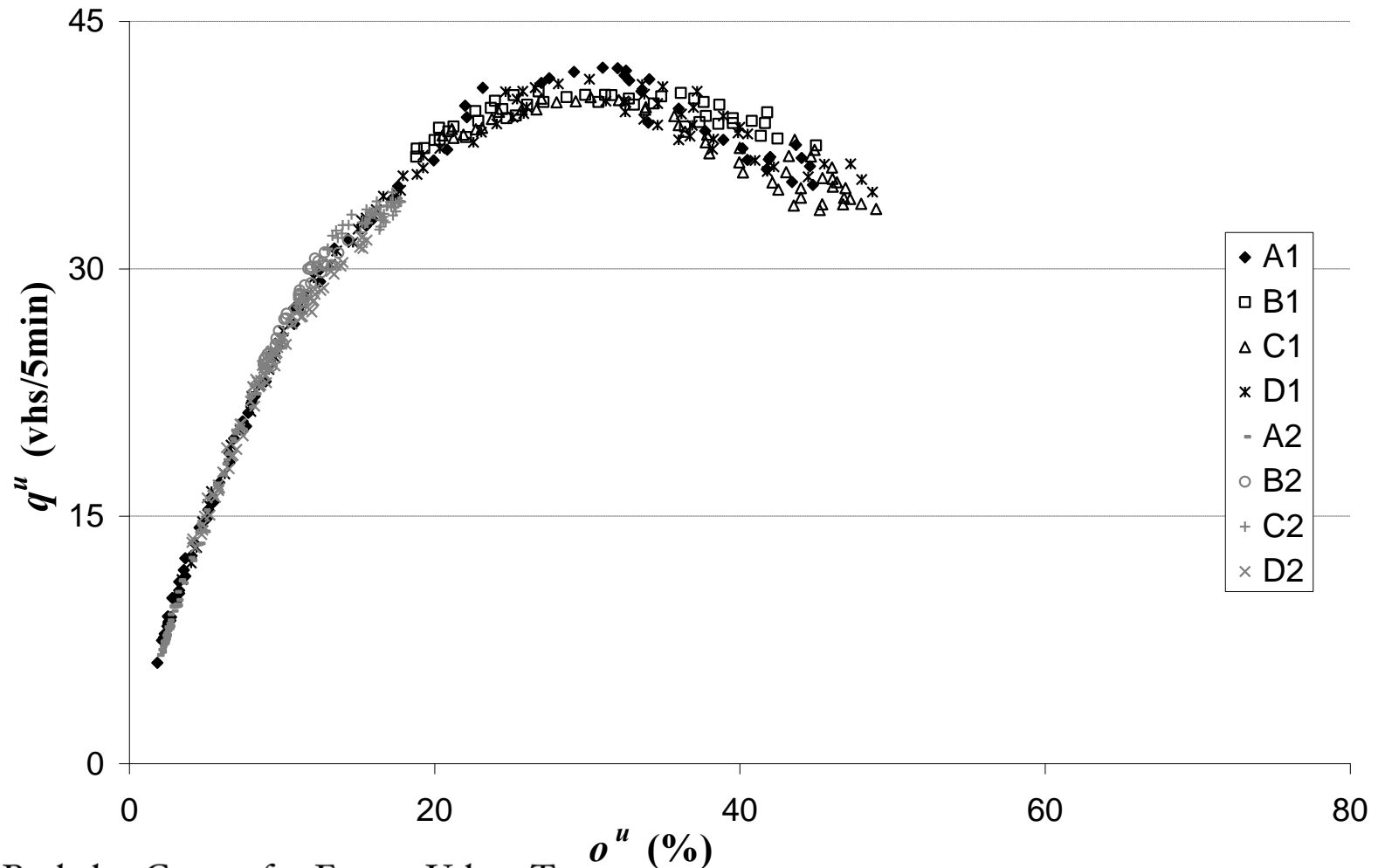
Then

- (a) VKT (i.e., average network flow) and VHT (i.e., average number of vehicles in network, average density or average occupancy) are related by MFD.
- (b) Trip completion rate/network flow(or VKT) \approx constant

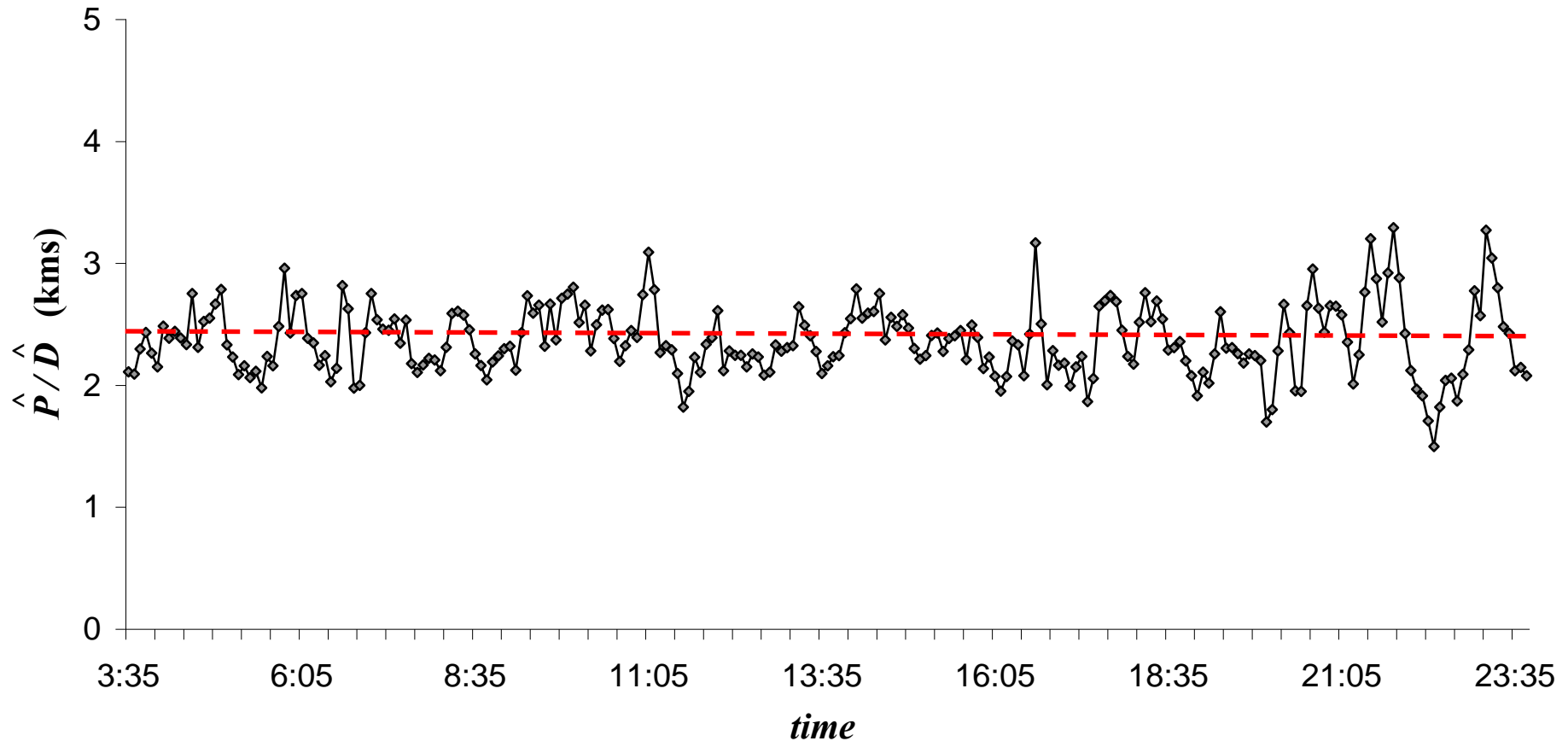
Real World Experiment: Yokohama, Japan



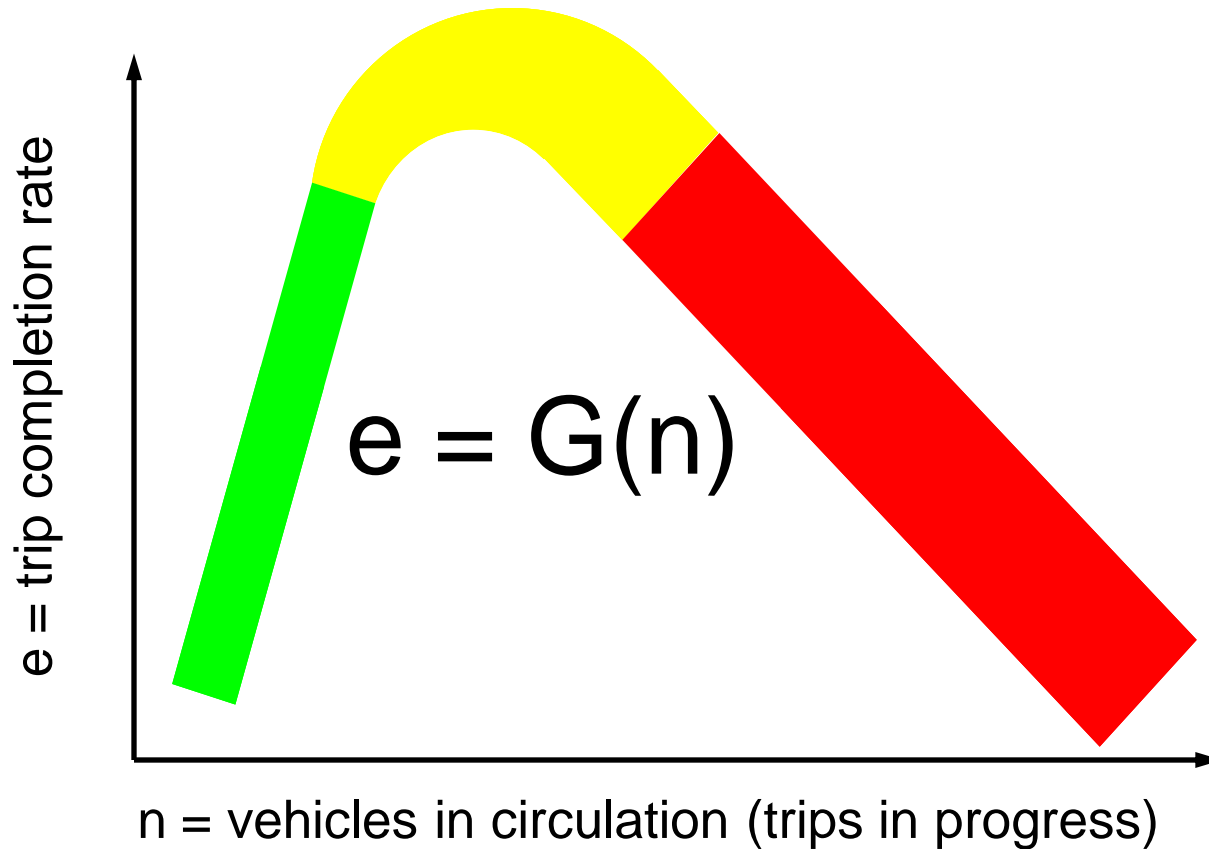
Experiment Result: Conjecture (a) MFD



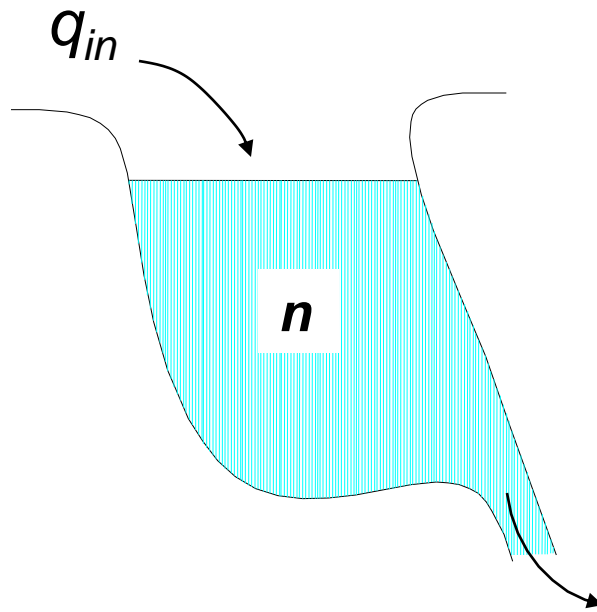
Experiment Result: Conjecture (b) Completion Rate Ratio



Application: Trips in progress vs. trips leaving



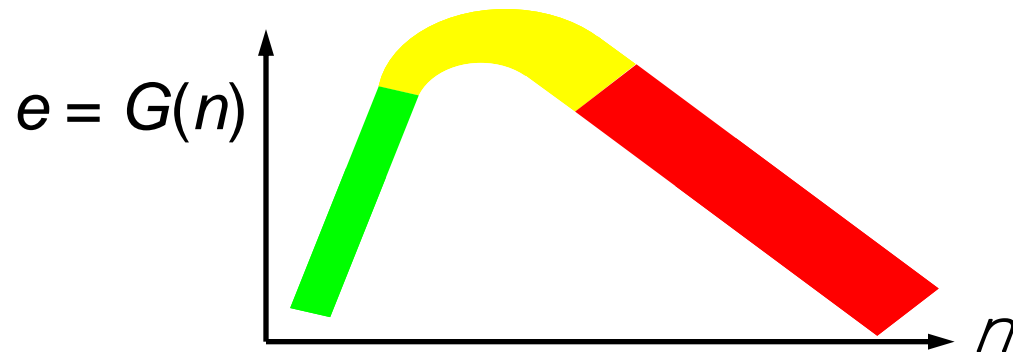
1-Bin Model: Aggregate Dynamics



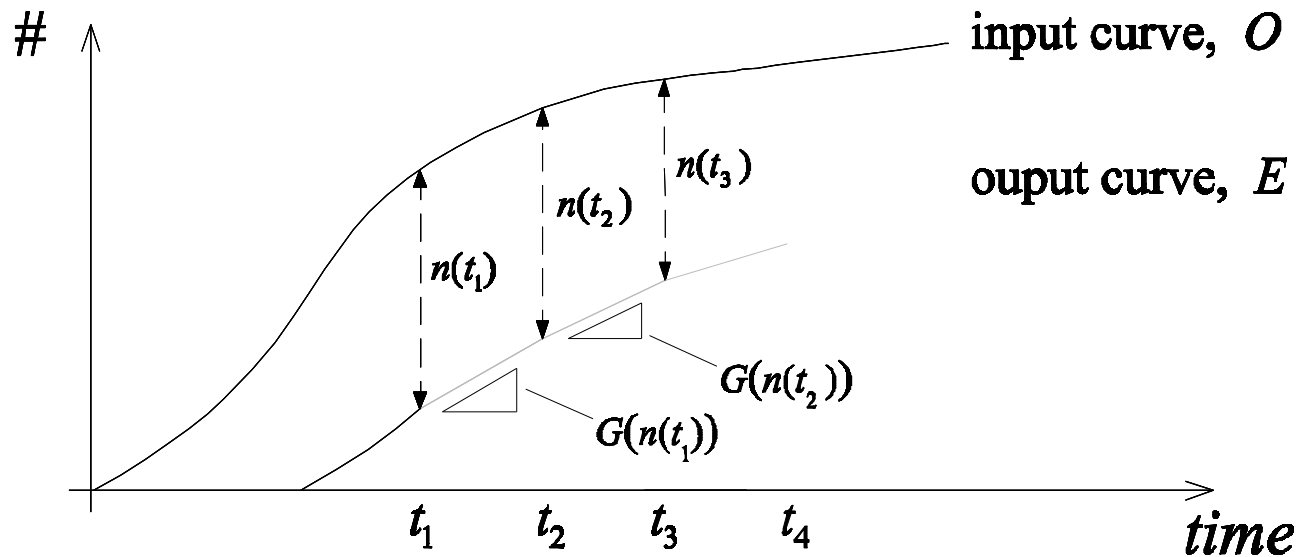
Given : inflow q_{in}

Output: $e = G(n)$

$$\frac{dn(t)}{dt} = q_{in}(t) - G(n(t))$$

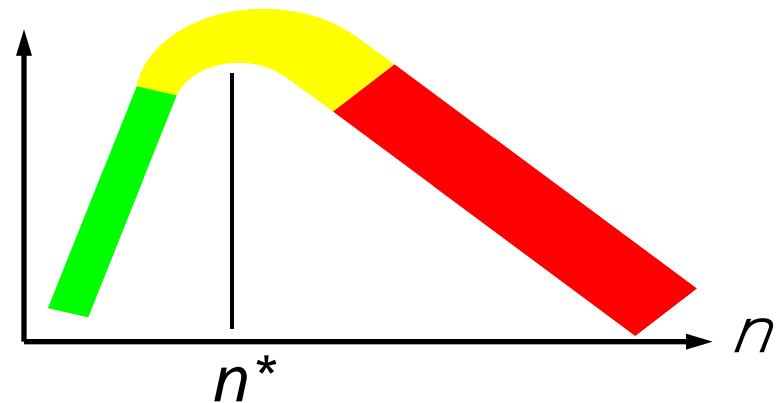
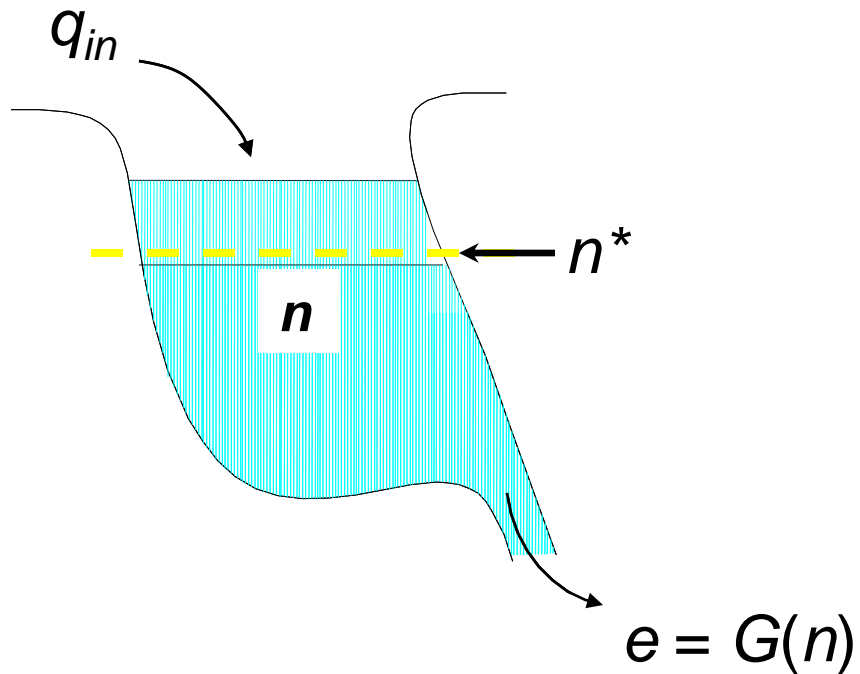


1-Bin Solution: Graphical Interpretation



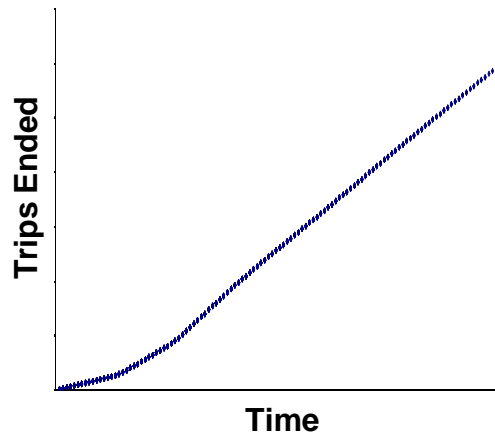
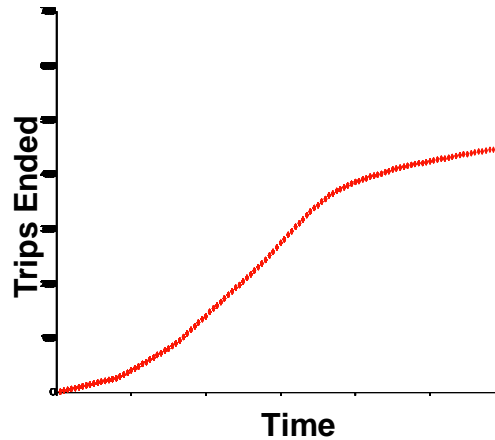
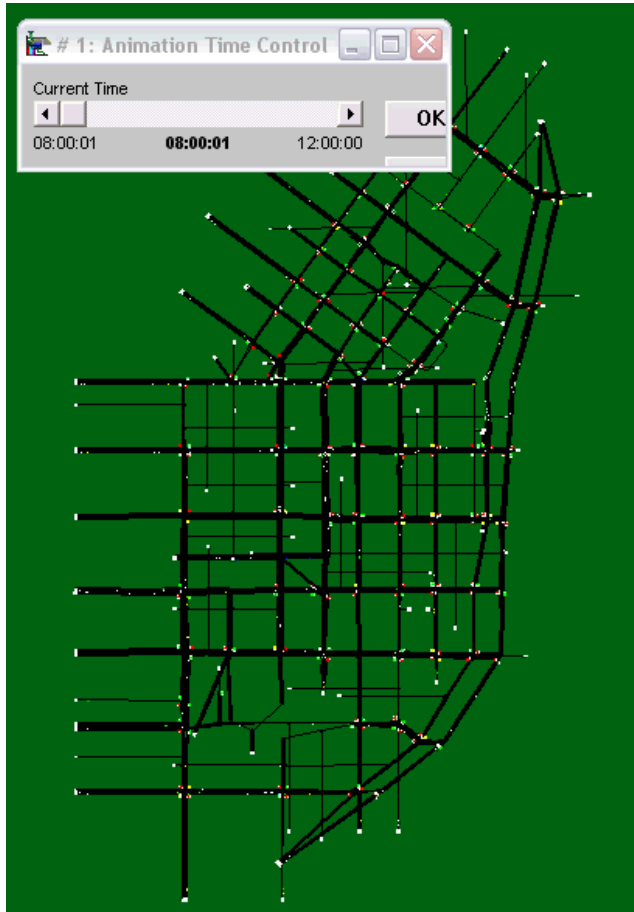
$$\frac{dn(t)}{dt} = O(t) - G(n(t))$$

1-Bin Model: Control Strategy

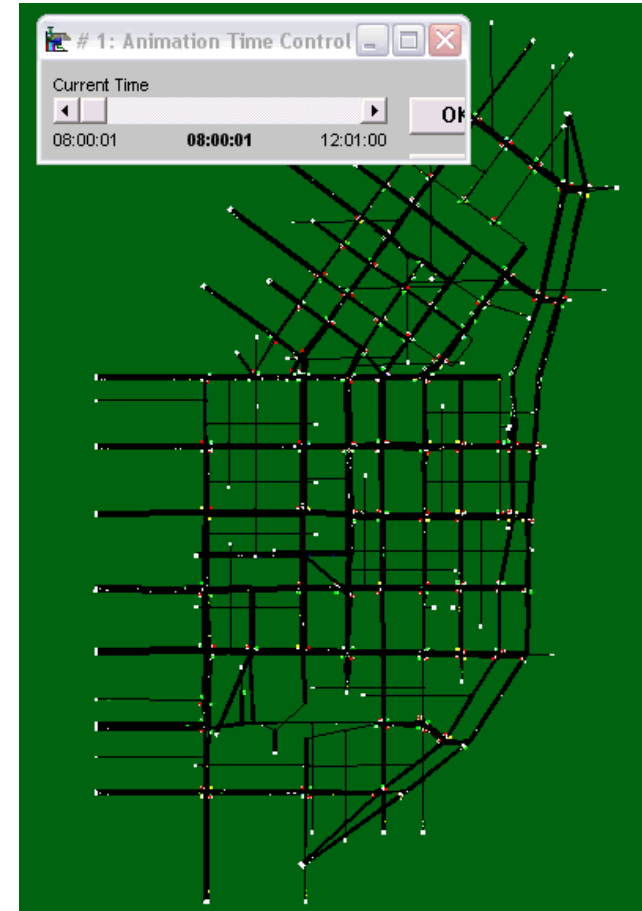


Application: Perimeter Control

No Control



With Control



Restrict vehicles from entering

(Geroliminis & Daganzo, 2007)

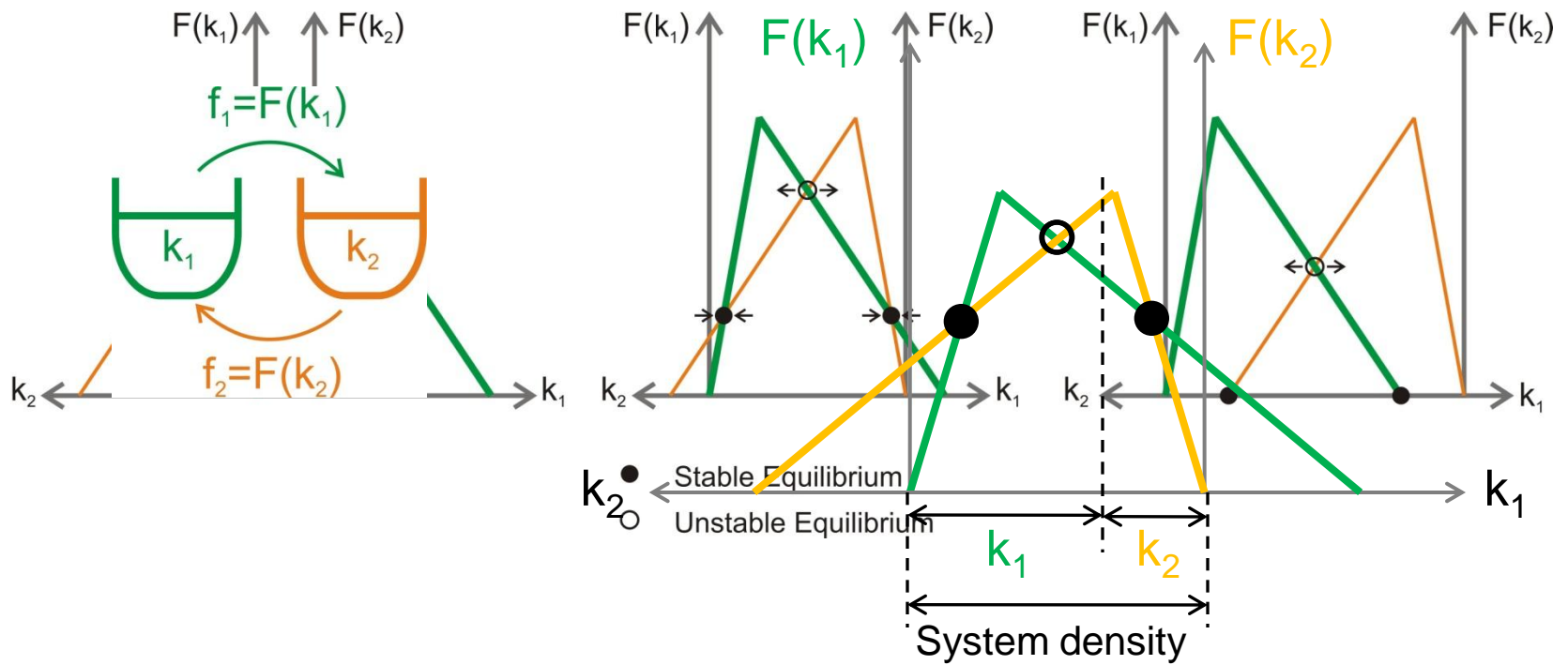
1-Bin Model: Caveats

- Conditions favoring an even distribution of traffic
 - Uniform demand
 - Homogeneous networks
 - Adaptive drivers
 - Redundant networks
 - Neighborhoods big but not too big
- Are there forces working against an even distribution?
 - Yes: congestion attracts congestion
But: Driver adaptation mitigates this effect

2-Ring Simulation

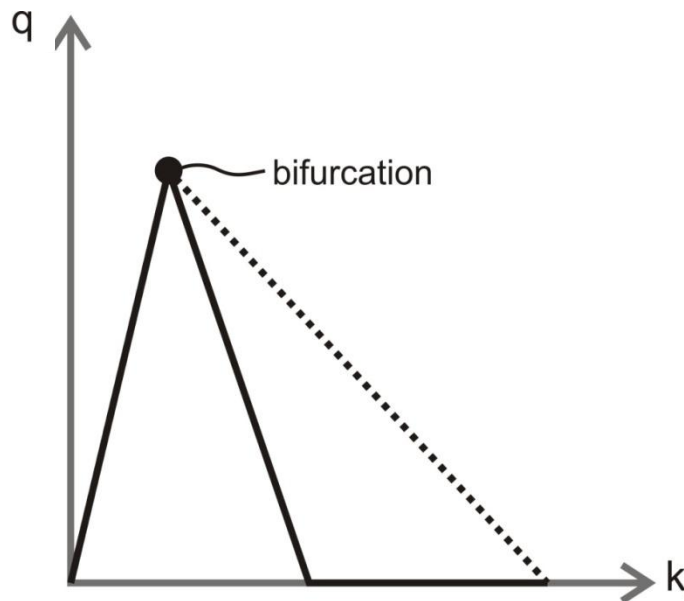
- http://www.ce.berkeley.edu/~daganzo/Simulations/two_ring_sim.html

Explanation: 2-Bin Model

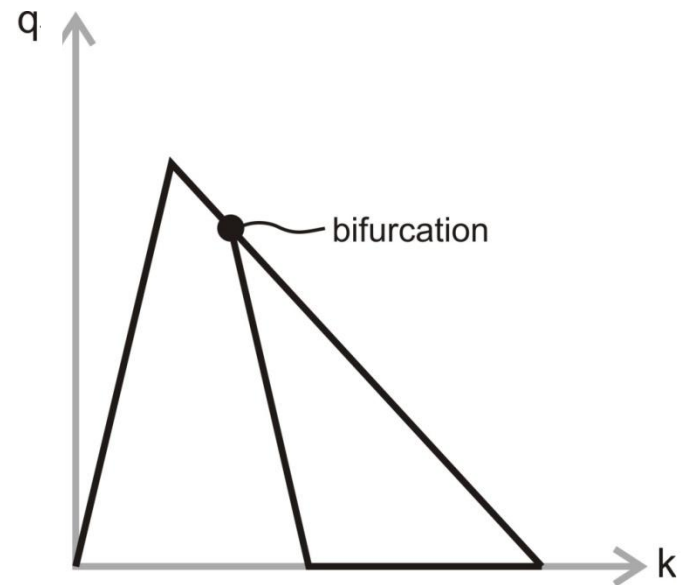


MFDs of 2-Bin Model

Non-adaptive drivers

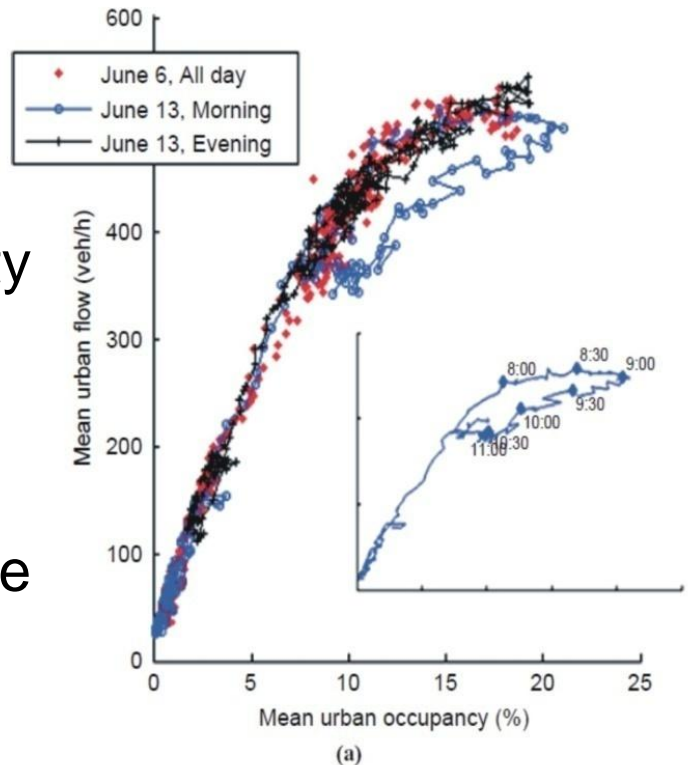


Adaptive drivers



Recent Findings

- Endogenous trip completion rates exacerbate effect and produce hysteresis loops beneath MFD.
- Hysteresis has been observed in reality (Buisson and Ladier, *JTRB* **2124**, 127-136, 2009)
- Yokohama's empirical evidence suggests that adaptation can overcome these problems for moderate congestion.

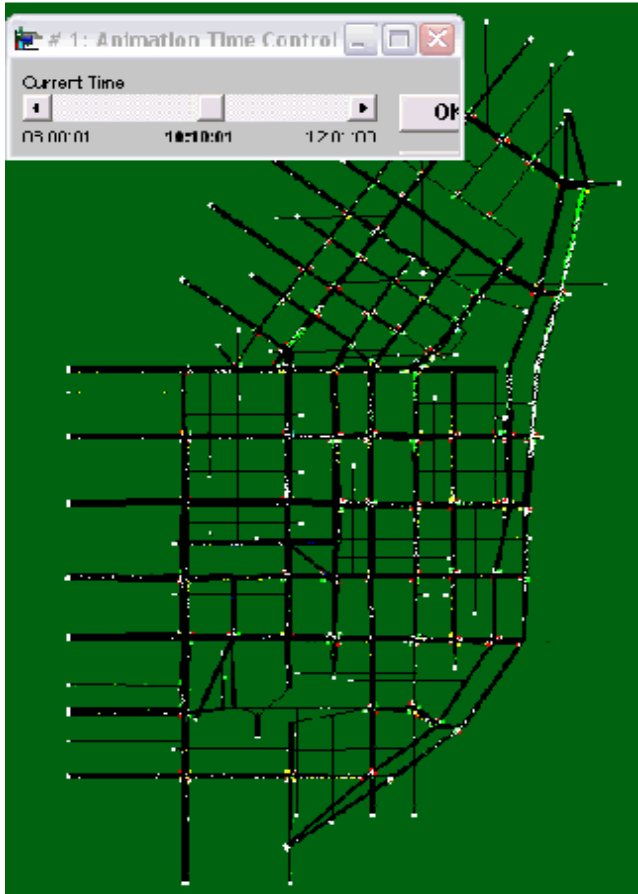


(Source: Buisson & Ladier, 2009)

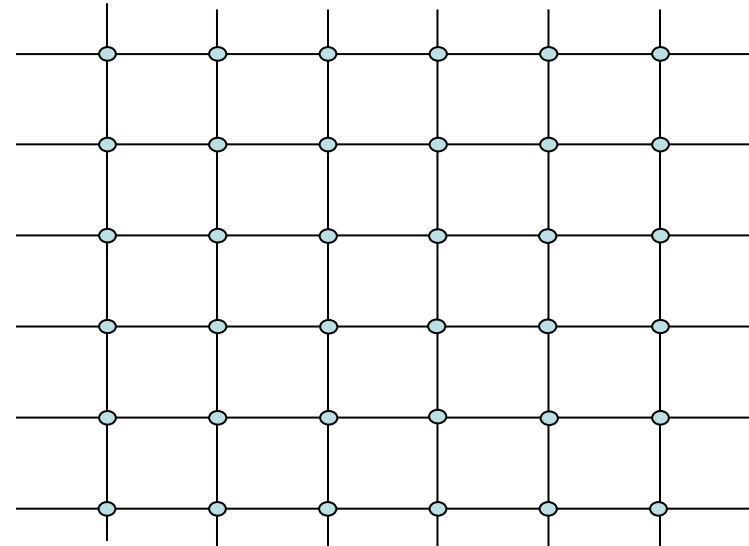
URBAN TRAFFIC: Summary

- Macroscopic models possible if vehicles distribute themselves evenly.
- Robust traffic management strategies are then possible.
- Homogeneous demand and driver adaptation even out the vehicular distribution
- Too much congestion can destroy evenness, reducing flow.
- Control strategies to redistribute traffic favorably should be considered.

Aggregate Models of Transit



Traffic Network

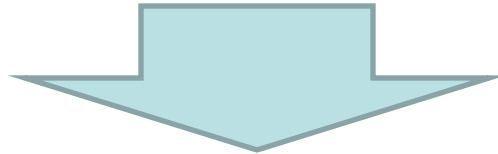


Transit Network



URBAN TRANSIT: Goal of Design Method

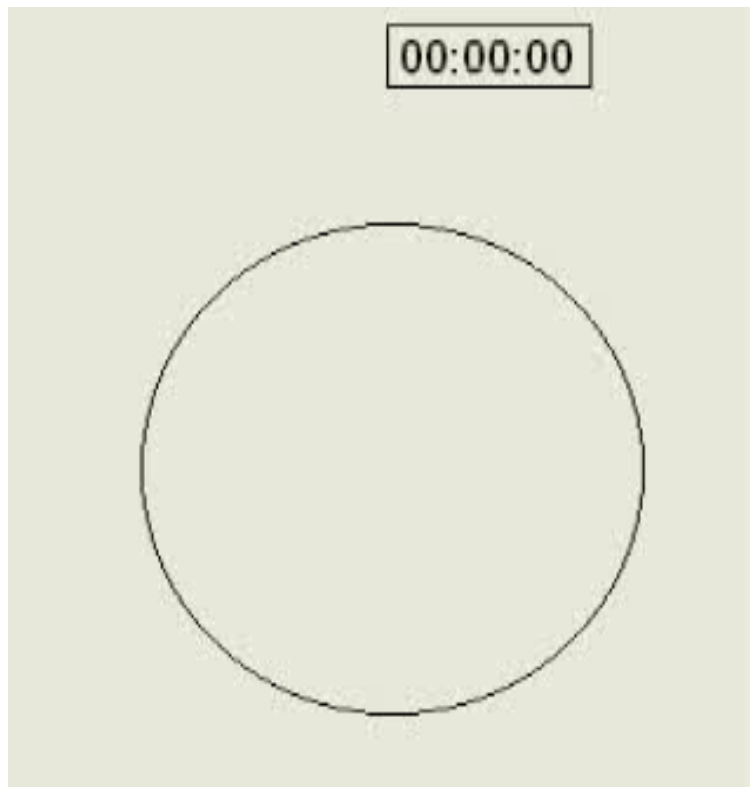
	When you want it?	Where you want it?	Quick?
<u>STATUS QUO</u>			
Individual Transportation (Auto)	YES	YES	YES
Public Transportation (Metro)	YES	NO	YES
Public Transportation (Bus)	NO	YES	NO



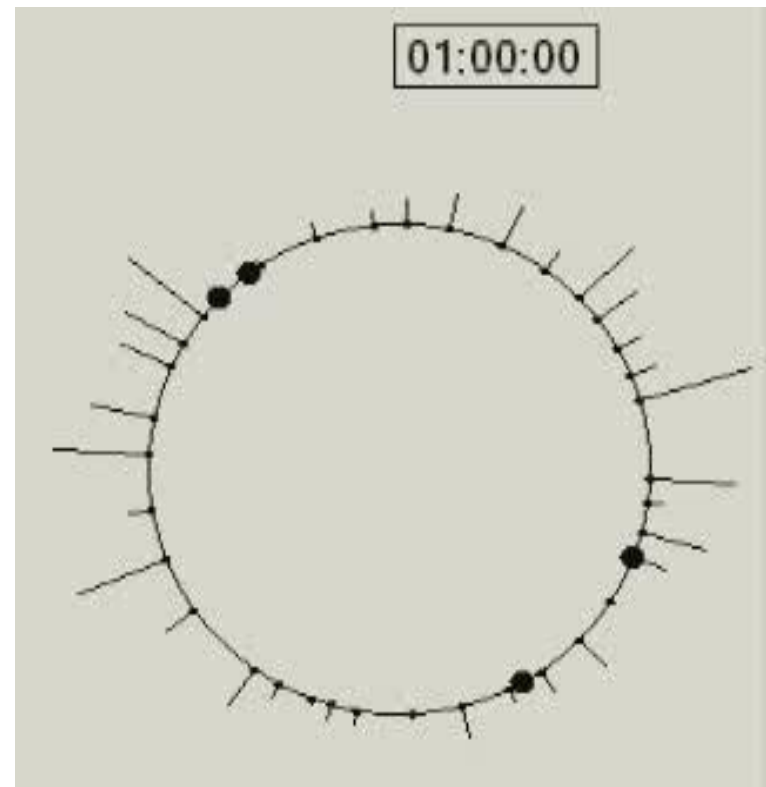
<u>VISION</u>			
Public Transportation (Next-gen Bus)	YES	YES	YES

The Spatial Distribution of Buses

4 Buses Uncontrolled



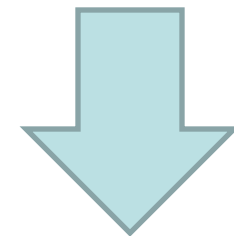
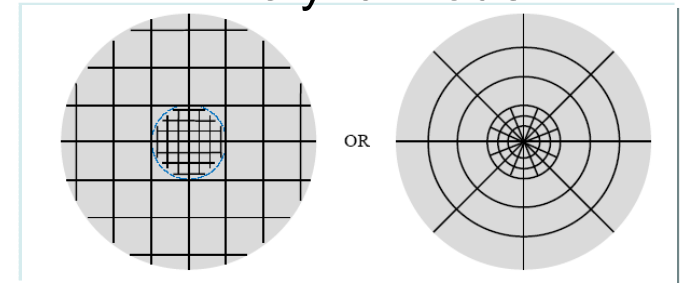
4 Buses Controlled



1-Bin Design Method

1. Define 2 decision variables for the network shape and the network density (i.e., the vehicular distribution inside the bin)
2. Define 1 decision variable for the headway or equivalently the fleet size (i.e., the number of buses in the bin)
3. Express society's welfare (combining passenger travel times and the agency costs) in terms of the 3 decision variables; and optimize.
4. Adapt the macroscopic 1-bin solution to the microscopic city details.

Analytic Model

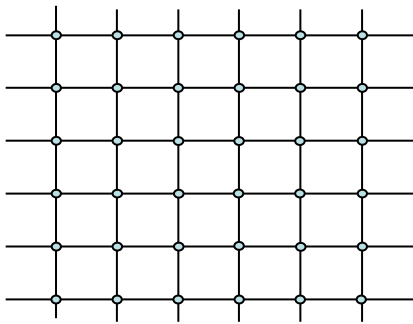


Real Solution



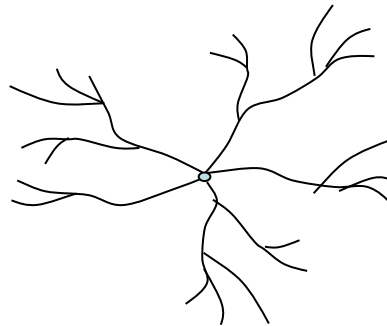
(Daganzo, 2010)

Network Shapes



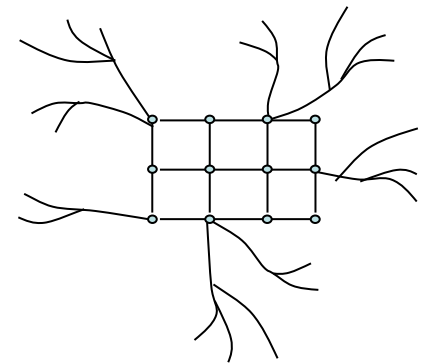
Grid

(Holroyd, 1965)



Radial

(Air Transport 1980's)



Hybrid

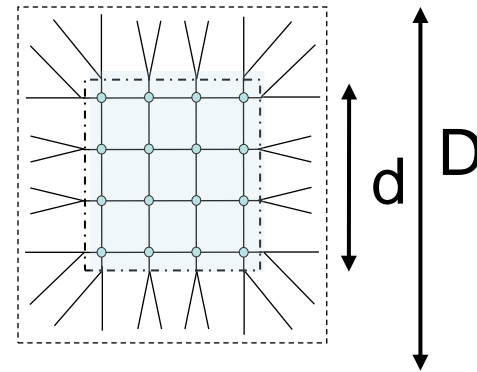
(Daganzo, 2010)

Decision Variable Definitions: Basic Concept

Headway (H)

Stop separation (s) = Line separation

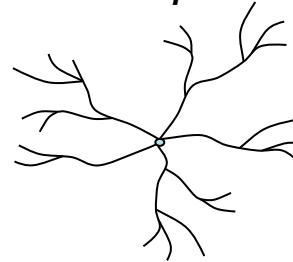
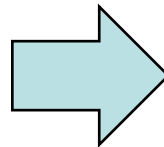
Ratio of central area, $\alpha=(d/D)$



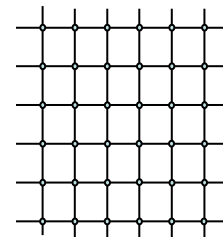
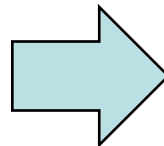
Basic Hybrid Structure

The hybrid concept can represent varied public transportation structures:

$\alpha=0$, radial



$\alpha=1$, grid

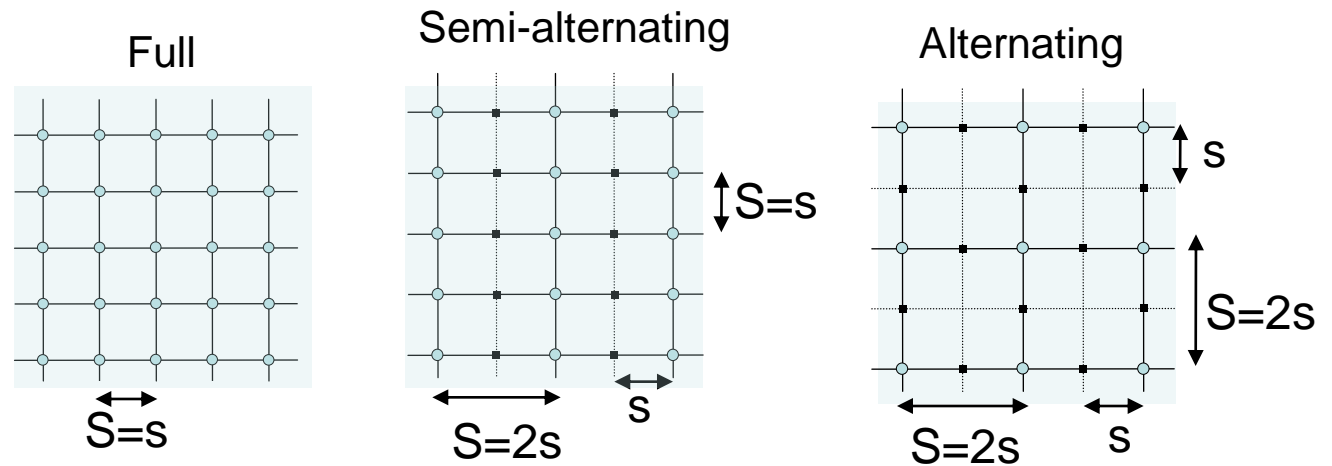


Generalized Concept

Additional variable

Line separation (S)

- Ordinary stop (no transfer)
- Transfer stop



1-Bin Model Formulation:

Objective function and decision variables

$$\min \left\{ Z = \underbrace{[\pi_V V + \pi_M M + \pi_L L]}_{\text{Agency time cost}} + \underbrace{[A + W + T + (\delta/v_w) e_T]}_{\text{User time cost}} : s \geq 0, H \geq 0, 0 \leq \alpha \leq 1, O \leq C \right\}$$

Agency costs (depend on α , s , H)

V	[veh-km/h]	Bus distance traveled per hour
M	[veh-h/h]	Fleet size
L	[km]	Length of two-way infrastructure
O	[pax/veh]	Maximum vehicle occupancy

User costs (depend on α , s , H)

A	[h]	Mean walking time
W	[h]	Mean waiting time
T	[h]	Mean riding time
e_T	[-]	Mean number of transfers
δ / v_w	[h]	Transfer Time

Optimal Design: Large City Results

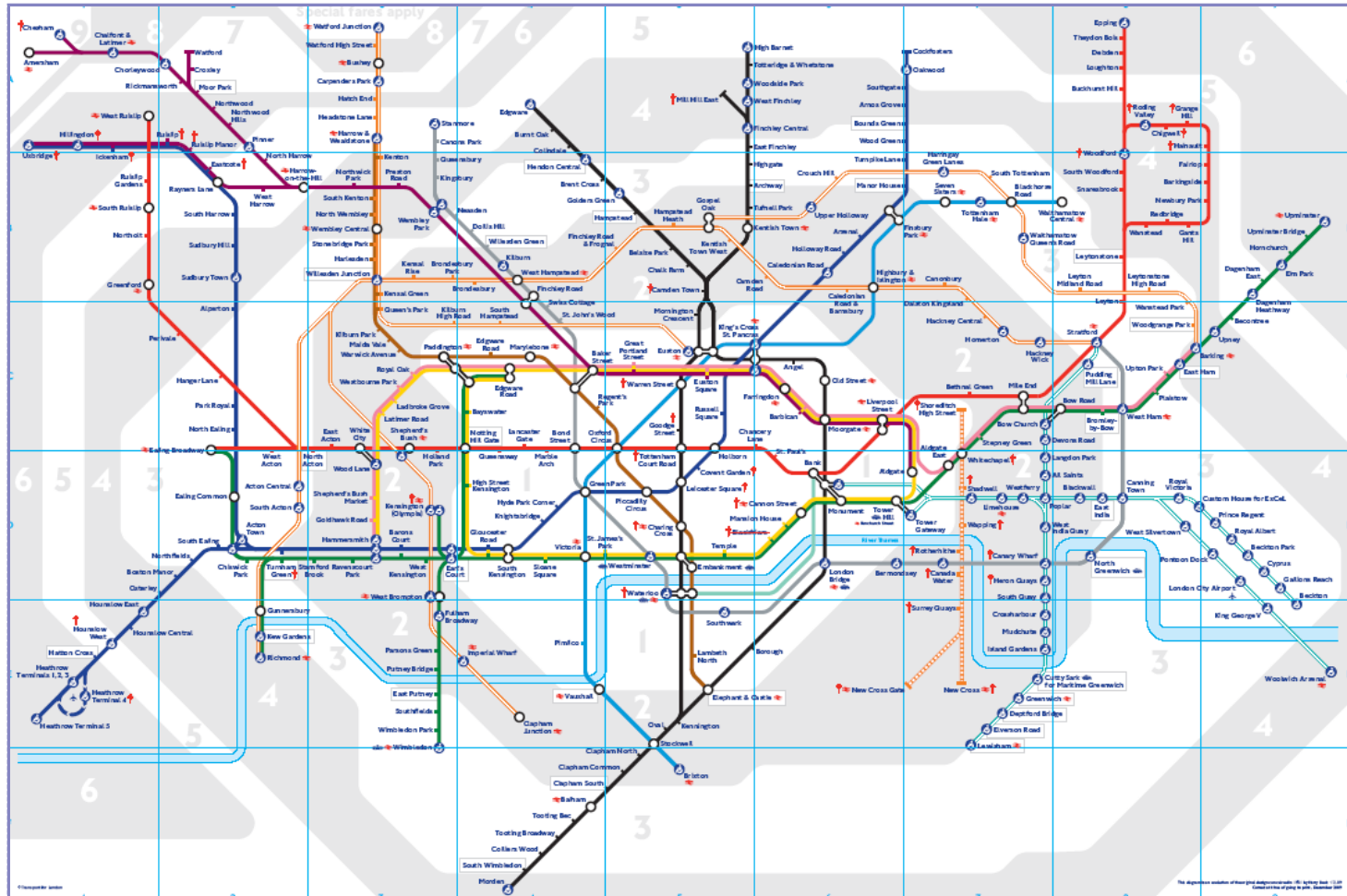
Typical parameter values for: Bus, BRT and Metro.

	C (p)	v (km/h)	\$_L (\$/km-h)	\$_V (\$/veh-km)	\$_M (\$/veh-h)
Bus	120	25	9	1	30
BRT	150	40	90	1	30
Metro	1000	60	900	3	40

Application to a large city (e.g., London, $I=80,000$ pax/h; $D=20$ km)

	α	s (km)	H (min)	O (pax)	M (veh)	v_c (km/h)	Z (min)
Bus	0.92	0.56	3.5	110	2627	17.8	71
BRT	0.83	0.61	3	150*	1882	25.1	62
Metro	0.57	1.05	2.5	396	724	35	88

London Metro



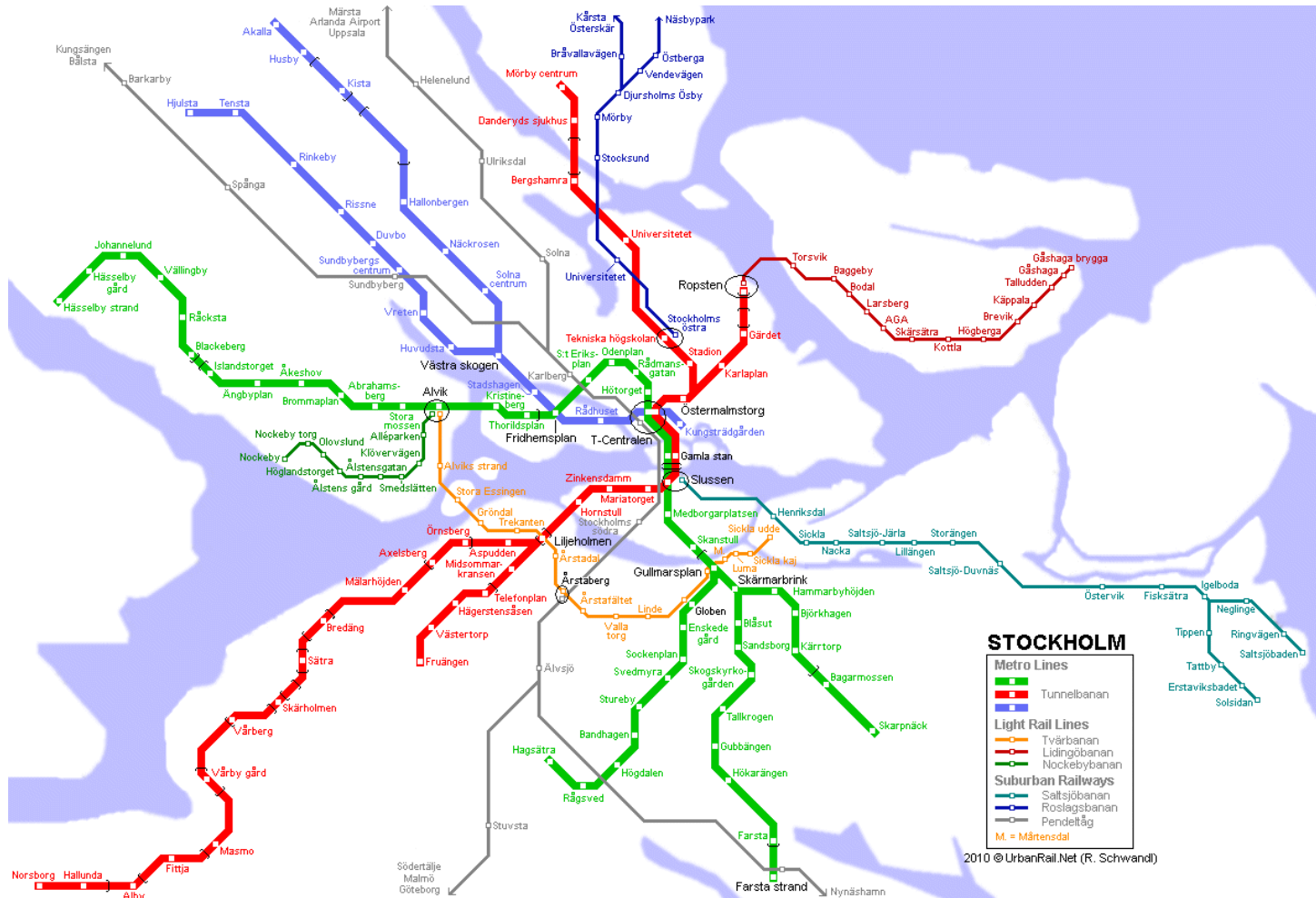
Optimal Design: Medium City Results

Application to a medium city

(e.g., Philadelphia $I=20,000$ pax/h; $D=10$ km)

	α	S (km)	H (min)	O (pax)	M (veh)	V_c (km/h)	Z (min)
Bus	0.94	0.47	5.0	65	599	16.5	51
BRT	0.81	0.53	4.0	95	437	23.0	49
Metro	0.38	0.97	3.0	314	121	33.8	75

Stockholm



Tokyo



Optimal Design: Medium City Results

Application to a medium city

(e.g., Philadelphia $I=20,000$ pax/h; $D=10$ km)

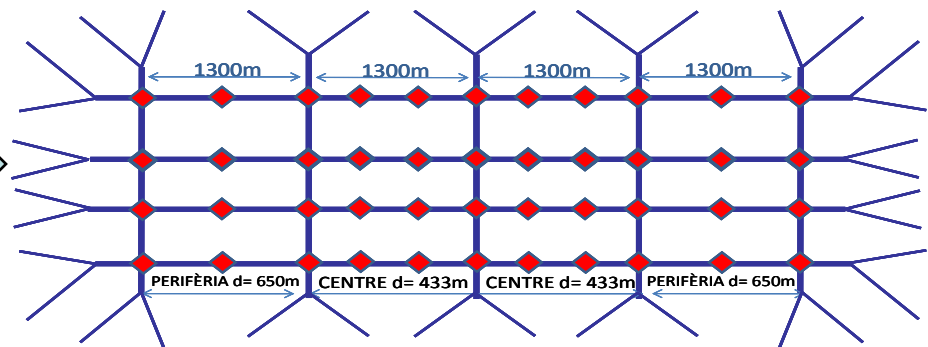
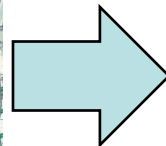
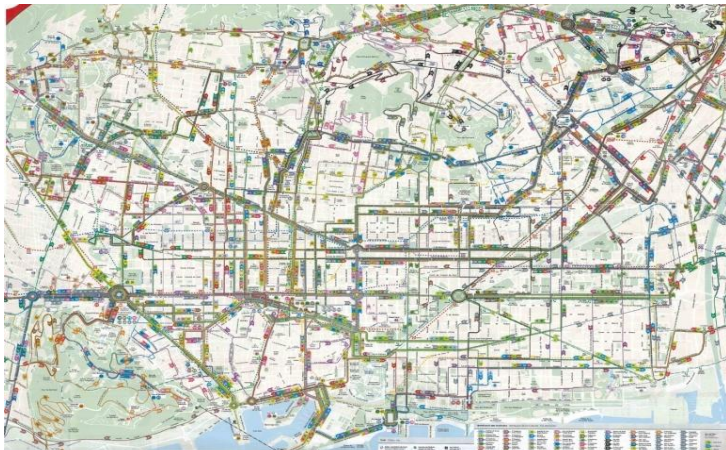
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South Chicago: Buses and Metro



Numerical Results for Barcelona: a 10x5 km rectangle

	Current bus system	Semi-alternating (no BRT, $v = 21$ km/h)
Door-to-door travel time (min)	57,9	50,3
Commercial speed (km/h)	11,9	15,1
Number of Buses	890	272
Stop separations (m)	300	650 (430 in the center)
Network shape $\alpha = a/A = b/B$	N.A.	0,80
Headway (min)	13	3

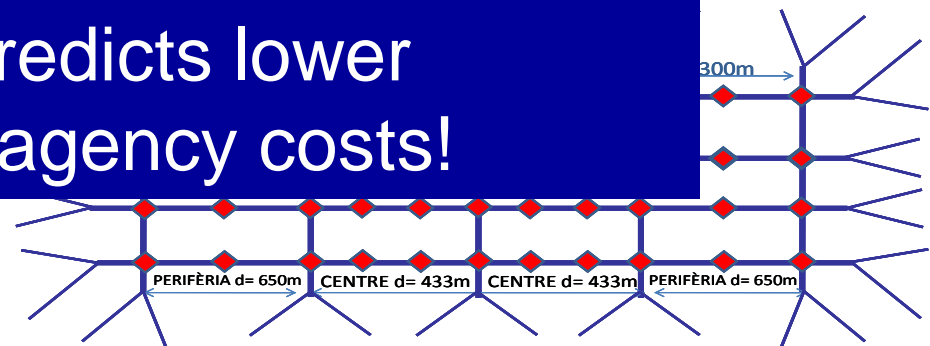


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Headway (min)	13	3



Model predicts lower
user and agency costs!



Final Design Step: From Macro to Micro



Simulations

- confirm the predicted savings
- match predictions to within 5%

Barcelona (2010-2011)



Ajuntament de Barcelona



References

1. Daganzo, C.F. (1996) "The nature of freeway gridlock and how to prevent it" in Transportation and Traffic Theory, Proc. 13th Int. Symp. Trans. Traffic Theory (J.B. Lesort, ed) pp. 629-646, Pergamon Elsevier, Tarrytown, N.Y.
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